

1. Use this function:  $k(w) = 6 - 10w$

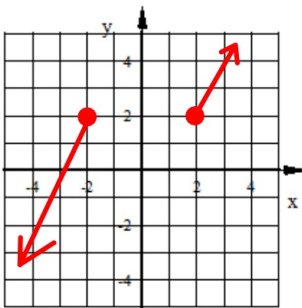
a) Find  $w$  if  $k(w) = 51$

$$51 = 6 - 10w$$
$$45 = -10w$$
$$w = -4.5$$

b) Find the Range for this Domain:  $\{-2, 0, 1, 2\}$

$$k(-2) = 6 - 10(-2) = 26$$
$$k(0) = 6 - 10(0) = 6$$
$$k(1) = 6 - 10(1) = -4$$
$$k(2) = 6 - 10(2) = -14$$

2. State the Domain and Range of this graph:



$$D: x \leq -2, x \geq 2$$
$$R: \mathbb{R}$$

3. Write a function rule for each table of values.

a)

X	Y
-5	21.5
-2	8.6
4	-17.2
6	-25.8
9	-38.7

$$y = mx$$

$$m = \frac{y}{x} = -4.3$$

$$y = -4.3x$$

b)

$$y = mx - 7$$

X	Y
-16	-75
-12	-58
0	-7
4	10
20	78

$$10 = 4m - 7$$

$$17 = 4m$$

$$m = 4.25$$

$$y = 4.25x - 7$$

### Section 5-5: Direct Variation

Direct Variation is a special Linear Function.

- It has a constant ratio  $\frac{Y}{X} = k$

$k$  = the Variation Constant

- Direct Variation Equation:

$$\frac{y}{x} = k \quad \text{or} \quad y = kx$$

## Graph of direct variation

- The graph must be a **line** that passes through **the origin**.

$\frac{y}{x}$  is a CONSTANT RATIO

4. Does each table represent Direct Variation?

If yes, state the variation constant and write a Direct Variation Equation.

a)

X	Y
-9	-28.35
-6	-18.9
-4	-12.6
5	15.75
14	44.1

3.15  
↓

Direct Variation?

If Yes,  $k =$

If yes, EQ:

yes  
3.15  
 $y = 3.15x$

b)

X	Y
13	31
15	28
17	25
19	22
21	19

Direct Variation?

If Yes,  $k =$

If yes, EQ:

no.

## Hwk #33 Answers:

12.  $y = -\frac{10}{8}x$  or  $-\frac{5}{4}x$

13.  $y = \frac{-9}{-5}x$  or  $\frac{9}{5}x$

23. EQ:  $E = 7.10h$

 $E = \text{Earnings}(\$)$   $h = \text{\#hrs}$ 

24. Yes. EQ:  $y = 1.8x$

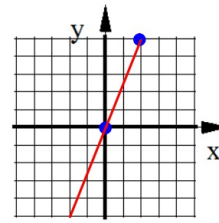
25. No

26. Yes. EQ:  $y = -1.5x$

37. a.

b.

41. EQ:  $y = \frac{5}{2}x = 2.5x$



45. a.  $k = \frac{5}{160} = 0.03125 \frac{\text{qt}}{\text{lb}}$

b.  $b = 0.03125w$

 $b = \text{amount of blood}$   $w = \text{weight}$   
qts lbs

c.

12.  $(-8, 10)$

13.  $(-5, -9)$

23. For the data in each table, tell whether  $y$  varies directly with  $x$ . Write an equation for the direct variation.

$x$	$y$
1	2
2	4
3	6
4	8

$x$	$y$
1	3
2	6
3	9
4	12

37. a. **Writing** How can you tell whether two sets of data represent a direct variation?

b. How can you tell if a line is the graph of a direct variation?

12	21.6
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8	11
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Graph the direct variation that includes the given points. Write an equation of the line.

41.  $(2, 5)$

42.  $(-2, 5)$

43.  $(2, -5)$

45. **Biology** The amount of blood in a person varies directly with weight. A person who weighs 160 lb has 5 quarts of blood.

a. Find the constant of variation.

b. Write an equation relating quarts of blood ( $b$ ) to weight ( $w$ ).c. **Open-Ended** Estimate the number of quarts of blood in a person who weighs 200 lb.

# 1.) Direct Variation Equations:

This Equation has a constant which means it CAN'T be written as  $y = kx$

$$\frac{y}{x} = k \quad \text{or} \quad y = kx$$

Is each equation direct variation?  
If yes, find the variation constant.

a.)  $-4 + 7x + 4 = 3y$  yes  $k = \frac{7}{3}$

$$7x = 3y$$

$$y = \frac{7}{3}x$$

b.)  $-10 + 2x + 1 = 3 + 4x - 2y$

$$-9 + 2x = 3 + 4x - 2y$$

$$-9 - 2x = 3 - 2y$$

$$-12 - 2x = -2y$$

$$y = 6 + 1x \quad \text{NO.}$$

## Direct Variation Equations:

$$\frac{y}{x} = k \quad \text{or} \quad y = kx$$

## 2.) Does each equation represent Direct Variation?

1.  $y - 3 = x$

NO.  $y = x + 3$

yes<sup>2.</sup>  $4y = -12x$

$y = -3x$

3.  $4x - 2y = 10$

NO.  $-4x - 2y = -4x + 10$

4.  $6x + 12y = 0$

yes.

- 3.) Given the table shows a direct variation relationship, find the value of ?.

To solve Direct Variation situations you can use either equation or you can use a Proportion

X	Y
-20	55
-12	33
?	-38.5
32	-88

①  $y = kx$   
 $k = 55 / -20$   
 $= -2.75$   
 $y = -2.75x$   
 $-38.5 = -2.75x$   
 $x = 14$

②  $\frac{55}{-20} = \frac{-38.5}{x}$   
 $55x = 770$   
 $x = 14$

The data below comes from a Direct Variation relationship.

X	Y
-5	-31.5
-2.4	-15.12
4.5	28.35
7	44.1
11	69.3

1. Write a Direct Variation Equation.

$k = 6.3$   $y = 6.3x$

2. Find x when y = 30

$30 = 6.3x$   
 $x = 4.76$

3. Find y when x = 20

$y = 6.3(20)$   
 $y = 126$

The given point is part of a Direct Variation relationship.

Write the equation for each Direct Variation relationship.

4.  $(9, 5)$   $y = .56x$   
 $y = \frac{5}{9}x$

5.  $(-4, 1)$   $y = -25x$   
 $y = -\frac{1}{4}x$

The ordered pairs are for the same Direct Variation relationship.

Write a direct variation equation then find the missing value.

6.  $(2, 5) \& (x, 16)$   $x = 6.4$   
 $\frac{5}{2} = \frac{16}{x}$   
 $5x = 32$

7.  $(10, y) \& (-3, 75)$   
 $\frac{y}{10} = \frac{75}{-3}$   
 $-3y = 750$   
 $y = -250$



Remember the phrase: "Y varies directly with X"

The number of tires a company can make varies directly with the number of employees at work that day. One recent day the company had 32 workers present and they produced 776 tires.

1. Find the Variation Constant,  
include units.

$$k = \frac{776}{32} = 24.25$$

tires/employee

2. Write a Direct Variation Equation.

$$y = 24.25x$$

3. Find the number of Employees that would be needed to make 1200 tires.

$$1200 = 24.25x$$

$$x = 50 \text{ employees.}$$



The amount of money raised varies directly with the number of people who contribute. \$1746 was raised when 24 people contributed.

1. Find the variation constant, including units.

$$k = \frac{1746}{24} = 72.75 \quad y = 72.75x$$

\$/person

2. Find the number of people it would take to raise \$10,000.

$$10,000 = 72.75x$$

$$x = 138 \text{ ppl.}$$

The amount of spaghetti required for a meal varies directly with the number of people that are served.

# of people served	lbs of Spaghetti
12	9
28	21
48	36
68	51

1. Find the variation constant including units.

$$k = 0.75 \quad y = 0.75x$$

lb/person

2. Find amount of spaghetti needed to feed 100 people.

$$y = 75 \text{ ppl.}$$

The point (4, -7) is on the graph of a direct variation relationship.

$(-4, 7)$

Write an equation for this Direct Variation.

$$y = \frac{7}{-4}x$$

Hwk #34 - Practice 5.5 Worksheet (due tomorrow)

IXL #13 - Q.2 & Q.10 due tomorrow at 4pm!