

What does a polynomial look like in Factored Form?

$(x-11)(2x+12)$ $\rightarrow$ When factoring, answers should look like these.
 $(x+7)(13x-12)(6x+4)$

1. Multiply $(x+4)(x+9)$ then factor $x^2 + 13x + 36$.

$$\begin{array}{r} x+4 \\ x \quad \boxed{\begin{array}{|c|c|} \hline x^2 & 4x \\ \hline 9x & 36 \\ \hline \end{array}} \\ +9 \end{array}$$

$$x^2 + 4x + 9x + 36$$

$$x^2 + 13x + 36$$

$$\downarrow$$

$$(x+4)(x+9)$$

2a. Multiply $(x-3)(x+11)$.

$$\begin{array}{r} x-3 \\ x \quad \boxed{\begin{array}{|c|c|} \hline x^2 & -3x \\ \hline 11x & -33 \\ \hline \end{array}} \\ +11 \end{array}$$

$$x^2 - 3x + 11x - 33$$

$$x^2 + 8x - 33$$

2b. What patterns do you notice between the numbers in the factored forms and the standard forms in the problems above? (ex: where did the 13 come from in #1?)

The #'s in factored form, $(x+4)(x+9)$, add to the "b" value ($4+9=13$) and multiply to the "c" value ($4 \cdot 9 = 36$)

3. Factor $x^2 - 12x + 32$

$$\begin{array}{r} 32 \leftarrow \text{"c"} \\ \wedge \\ -8 \cdot -4 \quad \text{"b"} \\ -8 + -4 = -12 \end{array}$$

$$\boxed{(x-8)(x-4)}$$

Factored Form

"a" ≠ 1 → Different Method

4. Factor $2x^2 - 9x - 5$

$$a \cdot c = -10$$

$$-10 \cdot 1$$

$$-10 + 1 = -9 \text{ "b"}$$

$$2x^2 - 10x + 1x - 5$$

$$2x(x - 5) + 1(x - 5)$$

$$(x - 5)(2x + 1)$$

5. Factor $3x^2 + 5x - 12$

$$a \cdot c = -36$$

$$9 \cdot -4$$

$$9 + -4 = 5$$

$$\begin{array}{r} \frac{?}{?} \end{array} \begin{array}{|c|c|} \hline 3x^2 & +9x \\ \hline -4x & -12 \\ \hline \end{array}$$

$$\begin{array}{r} \frac{x}{-4} \end{array} \begin{array}{|c|c|} \hline 3x^2 & +9x \\ \hline -4x & -12 \\ \hline \end{array}$$

$$GCF \left\{ \begin{array}{l} 3x \\ -4 \end{array} \right. \begin{array}{|c|c|} \hline 3x^2 & +9x \\ \hline -4x & -12 \\ \hline \end{array}$$

x above because
 $3x \cdot x = 3x^2$, 3 above
because $3x \cdot 3 = 9x$

$$(3x - 4)(x + 3)$$

You Try!

6. Factor $x^2 + 5x - 14$

7. Factor $4x^2 + 8x - 5$

8. Factor $x^2 - 81$ Hint: what is the "b" value?