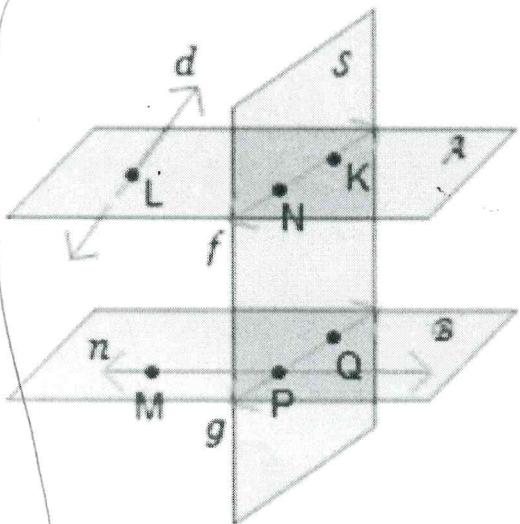


# Points, Lines, and Planes



- 1 Provide another name for Plane A: **Plane MKL**
- 2 Name the intersection of Plane A and line d **Point L**
- 3 Provide another name for line f: **fMK**
- 4 Name 4 coplanar points: **Points N, K, P, Q**
- 5 Name the intersection of Plane S and Plane A: **line f or MK**
- 6 Name the intersection of line n and line g: **Point P**
- 7 Name the intersection of Plane B and Plane S: **line g or PQ**
- 8 Name Plane S in two other ways: **Plane NKP and Plane NKQ**
- 9 Name 4 points that are non-coplanar: **N, K, M, P**
- 10 Name 3 points that are non-collinear: **L, M, K**
- 11 Name a point that is in both Plane S and Plane A: **Point N**
- 12 Name a point that is not in either Plane A or Plane S: **Point M**
- 13 Name a line that is contained in plane A: **line f or fMK**
- 14 Name a line that is not contained in Plane A: **line d**
- 15 Name a ray that is contained in Plane A: **MK**
- 16 Name a ray that is not contained in Plane A: **PM**

What are the two ways to name a plane?

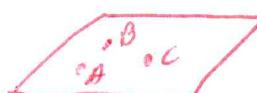
**① with the symbol in the corner of the plane  
② with 3 non-collinear points that lie in the plane**

What are the two ways to name a line?

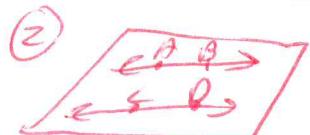
**① with the symbol next to the line  
② with any two points on the line with the arrows on top.**

Sketch each of the following independently:

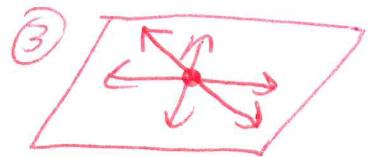
① Three points that are coplanar but not collinear.



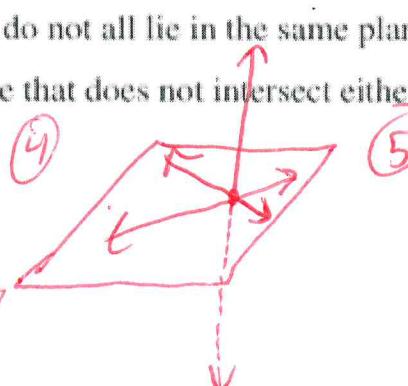
② Two lines that lie in a plane but do not intersect.



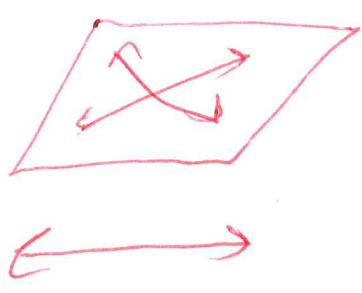
③ Three lines that intersect in a point and all lie in the same plane.



④ Three lines that intersect in a point but do not all lie in the same plane.



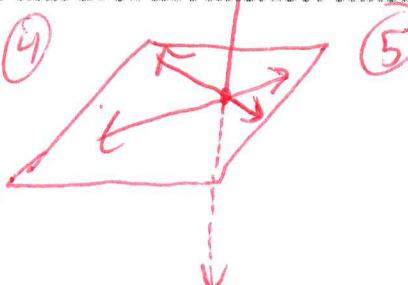
⑤ Two lines that intersect and another line that does not intersect either one.



⑥ Two planes that do not intersect.



⑦ Three planes that intersect in a line.



# Segment Addition/Segment bisectors

Find QR.

$$\begin{aligned} \overline{QT} &\cong \overline{TR} \\ \text{So } QT &= TR \\ 4x - 10 &= 78 \\ 4x - 10 + 10 &= 78 + 10 \\ 4x &= 88 \\ \frac{4x}{4} &= \frac{88}{4} \\ x &= 22 \end{aligned}$$

$$\begin{aligned} QT + TR &= QR \\ 78 + 78 &= QR \\ 156 &= QR \end{aligned}$$

**Using Midpoints** In the diagram below, B is the midpoint of  $\overline{AC}$ ,  $AB = 9$ , and  $AD = 25$ . Find  $CD$ .



$$\begin{aligned} \overline{AB} &\cong \overline{BC} \\ \text{So } BC &= 9 \text{ since } AC = 9 \\ AB + BC + CD &= 25 \\ 9 + 9 + CD &= 25 \\ 18 + CD &= 25 \end{aligned}$$

$$\begin{aligned} 18 + CD &= 25 \\ -18 &-18 \\ CD &= 7 \end{aligned}$$

Given B is between A and C. If  $AC = x + 10$ ,  $AB = 5x$ , and  $BC = 3x - 4$  find the values of  $x$  and  $AC$ .

$$\begin{aligned} \overbrace{5x}^{\text{AB}} + \overbrace{3x - 4}^{\text{BC}} &= x + 10 \\ 5x + 3x - 4 &= x + 10 \\ 8x - 4 &= x + 10 \\ -x &-x \\ 7x - 4 &= 10 \\ +4 &+4 \\ 7x &= 14 \\ \frac{7x}{7} &= \frac{14}{7} \\ x &= 2 \end{aligned}$$

Given:  $AC = 39$  m

$$\begin{aligned} A &\quad B &\quad C \\ 2x - 8 & & x + 17 \\ \hline 39 & & \end{aligned}$$

$$\begin{aligned} x &= 10 \\ AB &= 12 \\ BC &= 27 \end{aligned}$$

$$\begin{aligned} AB + BC &= AC \\ 2x - 8 + x + 17 &= 39 \\ 3x + 9 &= 39 \\ -9 &-9 \\ 3x &= 30 \\ \frac{3x}{3} &= \frac{30}{3} \\ x &= 10 \end{aligned}$$

$$\begin{aligned} BC &= x + 17 \\ BC &= 10 + 7 \\ BC &= 27 \end{aligned}$$

$$\begin{aligned} 5x + 3x - 4 &= x + 10 \\ 8x - 4 &= x + 10 \\ -x &-x \\ 7x - 4 &= 10 \\ +4 &+4 \\ 7x &= 14 \\ \frac{7x}{7} &= \frac{14}{7} \\ x &= 2 \end{aligned}$$

Identify the segment bisector of  $\overline{PQ}$ . Then find  $PQ$ .

$$\begin{aligned} 5(3) - 7 &= 8 & 14 - 2(3) &= 8 \\ \text{So } PM &= MQ \\ 5x - 7 &= 8 & 14 - 2x &= 8 \\ +2x &+2x \\ 7x - 7 &= 14 - 2x & 14 &= 14 \\ +2x &+2x \\ 9x &= 21 & & \\ \frac{9x}{9} &= \frac{21}{9} & & \\ x &= 3 & & \end{aligned}$$

$$\begin{aligned} PQ &= 16 & PM + MQ &= PQ \\ 8 + 8 &= PQ & 7x - 7 &= 14 \\ 16 &= PQ & +7 &+7 \\ & & 7x &= 21 \end{aligned}$$

Find DE and EF.

$$\begin{aligned} D &\quad E &\quad F \\ 9 & & 9 \\ \hline 18 & & \end{aligned}$$

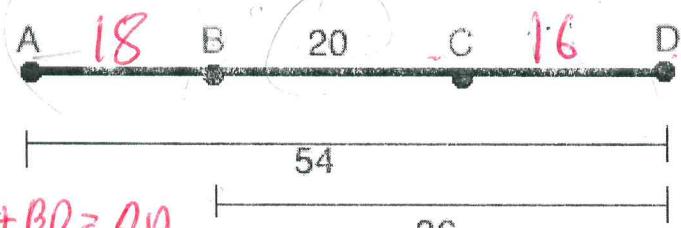
$$\begin{aligned} \overline{DB} &\cong \overline{EF} \\ \text{So } DB &= BF \\ 9 &= 9 \end{aligned}$$

$$\begin{aligned} DB + FP &= DP \\ DB + DB &= DP \\ 2DB &= DP \\ \frac{2DB}{2} &= \frac{DP}{2} \\ DB &= \frac{DP}{2} \end{aligned}$$

$$\begin{aligned} DB + FP &= DP \\ DB + DB &= DP \\ 2DB &= DP \\ \frac{2DB}{2} &= \frac{DP}{2} \\ DB &= \frac{DP}{2} \end{aligned}$$

# Segment Addition Higher Level

Find AB and CD:



$$BC + CD = BD$$

$$20 + CD = 36$$

$$-20 \quad -20$$

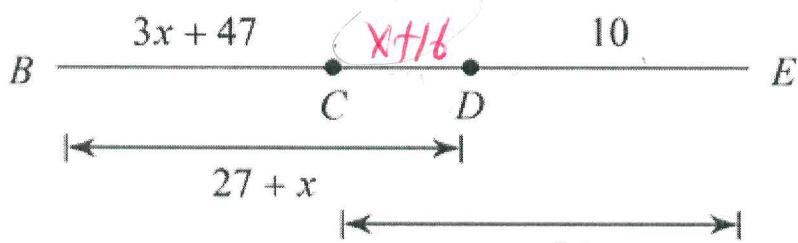
$$\boxed{CD = 16}$$

$$AB + BD = AD$$

$$AB + 36 = 54$$

$$\cancel{\begin{array}{r} 36 \\ AB \\ \hline 18 \end{array}}$$

Find CE



$$CD + DE = CE$$

$$CD + 10 = x + 26$$

$$-10 \quad -10$$

$$\boxed{CD = x + 16}$$

$$BC + CD = BD$$

$$3x + 47 + x + 16 = 27 + x$$

$$4x + 63 = 27 + x$$

$$-x \quad -x$$

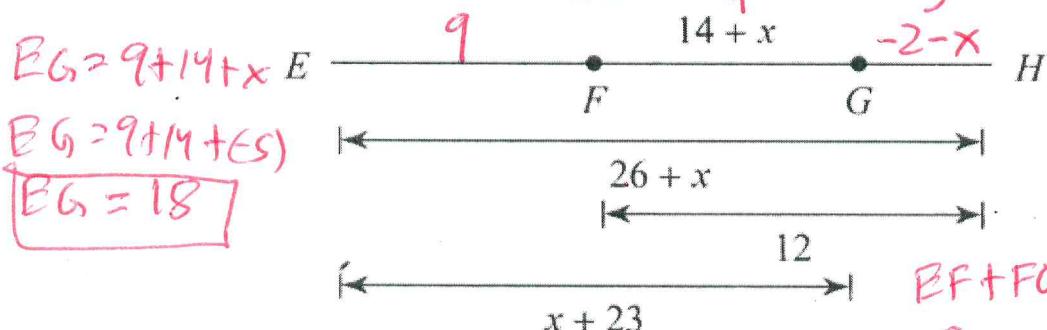
$$3x + 63 = 27$$

$$-63 \quad -63$$

$$\frac{3x}{3} = \frac{-36}{3}$$

$$\boxed{x = -12}$$

Find EG



$$EF + FG + GH = EH$$

$$\underline{9 + 14 + x + -2 - x = 26 + x}$$

$$EF + FG = EG$$

$$9 + 14 + x = 23$$

$$-14 - x \quad -x - 14$$

$$\boxed{BF = 9}$$

$$FG + GH = FH$$

$$14 + x + -2 - x = 12$$

$$-14 - x \quad -14 - x$$

$$GH = -2 - x$$

$$21 = 26 + x$$

$$-26 \quad -26$$

$$\boxed{-5 = x}$$

# Midpoint/Distance Formulas

Given points A(-4, 2) and B(3, 3).

1. If C is the midpoint of AB, find point C.
2. Find AB.
3. If B is the midpoint of AD, find point D.

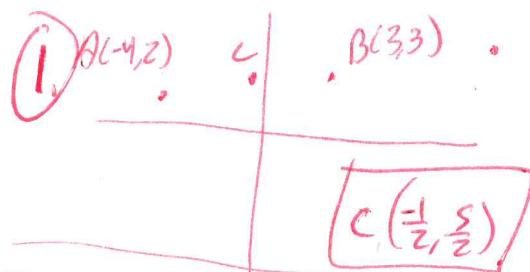
Give the points A(3, -2) and B(-5, 6).

4. Find the midpoint C of the two points.

5. Find AC

6. Find BC

7. If (3, -2) is an endpoint and (-5, 6) is a midpoint, find the other endpoint.



(1)  $A(-4, 2)$   $B(3, 3)$

$$AB = \sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2}$$

$$AB = \sqrt{(-4 - 3)^2 + (2 - 3)^2}$$

$$AB = \sqrt{(-7)^2 + (-1)^2}$$

$$AB = \sqrt{49 + 1}$$

$$\boxed{AB = \sqrt{50}}$$

(6)  $B(-5, 6)$   $C(-1, 2)$

$$BC = \sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2}$$

$$BC = \sqrt{(-5 - -1)^2 + (6 - 2)^2}$$

$$BC = \sqrt{(-4)^2 + 4^2}$$

$$BC = \sqrt{16 + 16}$$

$$\boxed{BC = \sqrt{32}}$$

(4)  $A(-4, 2)$   $B(3, 3)$

$$x_m = \frac{x_1 + x_2}{2} \quad y_m = \frac{y_1 + y_2}{2}$$

$$x_m = \frac{-4 + 3}{2} \quad y_m = \frac{2 + 3}{2}$$

$$x_m = \frac{-1}{2} \quad y_m = \frac{5}{2}$$

(4)  $A(3, -2)$   $B(-5, 6)$

$$x_m = \frac{x_1 + x_2}{2} \quad y_m = \frac{y_1 + y_2}{2}$$

$$x_m = \frac{3 + -5}{2} \quad y_m = \frac{-2 + 6}{2}$$

$$x_m = \frac{-2}{2} \quad y_m = \frac{4}{2}$$

$$\boxed{C(-1, 2)}$$

(3)  $A(-4, 2)$   $B(3, 3)$   $D(x_2, y_2)$

$$x_m = \frac{x_1 + x_2}{2} \quad y_m = \frac{y_1 + y_2}{2}$$

$$3 = \frac{-4 + x_2}{2} \quad 3 = \frac{2 + y_2}{2}$$

$$6 = -4 + x_2 \quad 6 = 2 + y_2$$

$$10 = x_2 \quad 4 = y_2$$

$$\boxed{D(10, 4)}$$

(5)  $A(3, -2)$   $C(-1, 2)$

$$AC = \sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2}$$

$$AC = \sqrt{(3 - -1)^2 + (2 - -2)^2}$$

$$AC = \sqrt{(4)^2 + 4^2}$$

$$AC = \sqrt{16 + 16}$$

$$\cancel{AC = \sqrt{32}}$$

$$\boxed{AC = \sqrt{32}}$$

(7)  $(3, -2)$   $(-5, 6)$   $(x_2, y_2)$

$$x_m = \frac{x_1 + x_2}{2} \quad y_m = \frac{y_1 + y_2}{2}$$

$$-5 = \frac{3 + x_2}{2} \quad 6 = \frac{-2 + y_2}{2}$$

$$-10 = 3 + x_2 \quad 12 = -2 + y_2$$

$$-13 = x_2 \quad 14 = y_2$$

$$\boxed{(-13, 14)}$$