

Answer Key

1. $TU = 2x$, $UB = 3x + 1$, $TB = 21$

2. $TU = 4x - 1$, $UB = 2x - 1$, $TB = 5x$

$$\begin{aligned} TU + UB &= TB \\ 2x + 3x + 1 &= 21 \\ 5x + 1 &= 21 \\ 5x &= 20 \\ x &= 4 \end{aligned}$$

$$\begin{aligned} TU &= 2x \\ &= 2(4) \\ &= 8 \\ UB &= 3x + 1 \\ &= 3(4) + 1 \\ &= 12 + 1 \\ &= 13 \end{aligned}$$

$$\begin{aligned} x &= 4 \\ TU &= 8 \\ UB &= 13 \end{aligned}$$

$$\begin{aligned} TU + UB &= TB \\ 4x - 1 + 2x - 1 &= 5x \\ 6x - 2 &= 5x \\ 6x - 5x &= 2 \\ x &= 2 \end{aligned}$$

$$\begin{aligned} TU &= 4x - 1 \\ &= 4(2) - 1 \\ &= 8 - 1 \\ &= 7 \\ UB &= 2x - 1 \\ &= 2(2) - 1 \\ &= 4 - 1 \\ &= 3 \end{aligned}$$

$$\begin{aligned} x &= 2 \\ TU &= 7 \\ UB &= 3 \\ TB &= 10 \end{aligned}$$

Write an equation for the each: $\overline{AB} \cong \overline{BC}$

3. Segment AB is congruent to segment BC $\overline{AB} = \overline{BC}$

4. $\overline{XY} \cong \overline{AB}$ $\overline{XY} = \overline{AB}$

5. Point B bisects segment AC $\overline{AB} = \overline{BC}$

6. $2x + 5$ is equal to $4x - 8$ $2x + 5 = 4x - 8$

7. Point A is the midpoint of segment PT $\overline{PA} = \overline{AT}$

$$\begin{aligned} TB &= TU + UB \\ TB &= 7 + 3 \\ TB &= 10 \end{aligned}$$

For 8 and 9 suppose $\overline{RS}$ is congruent to $\overline{MN}$. For each set of lengths, solve for x , and find the length of each segment. For 10-12, $\overline{AB} \cong \overline{BC}$.

8. $RS = 3x + 17$, $MN = 7x - 15$

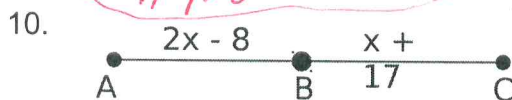
9. $RS = x + 10$, $MN = 2x + 4$

$$\begin{aligned} RS &= MN \\ 3x + 17 &= 7x - 15 \\ -3x & \quad -3x \\ 17 &= 4x - 15 \\ +15 & \quad +15 \\ 32 &= 4x \\ 8 &= x \end{aligned}$$

$$\begin{aligned} RS &= 3x + 17 \\ &= 3(8) + 17 \\ &= 24 + 17 \\ &= 41 \\ MN &= 7x - 15 \\ &= 7(8) - 15 \\ &= 56 - 15 \\ &= 41 \end{aligned}$$

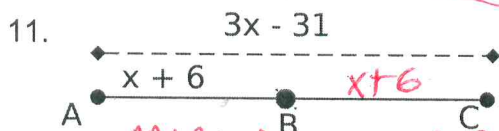
$$\begin{aligned} RS &= MN \\ x + 10 &= 2x + 4 \\ -x & \quad -x \\ 10 &= x + 4 \\ -4 & \quad -4 \\ 6 &= x \end{aligned}$$

$$\begin{aligned} RS &= x + 10 \\ &= 6 + 10 \\ &= 16 \\ MN &= 2x + 4 \\ &= 2(6) + 4 \\ &= 12 + 4 \\ &= 16 \end{aligned}$$



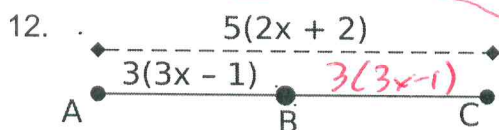
$$\begin{aligned} \overline{AB} &\cong \overline{BC} \\ 2x - 8 &= x + 17 \\ +8 & \quad +8 \\ 2x &= x + 25 \\ -x & \quad -x \\ x &= 25 \end{aligned}$$

$$\begin{aligned} AB &= 2x - 8 \\ &= 2(25) - 8 \\ &= 50 - 8 \\ &= 42 \\ BC &= x + 17 \\ &= 25 + 17 \\ &= 42 \end{aligned}$$



$$\begin{aligned} \overline{AB} &\cong \overline{BC} \\ x + 6 &= 3x - 31 \\ -2x & \quad -2x \\ 37 &= 2x \\ 18.5 &= x \end{aligned}$$

$$\begin{aligned} AB &= x + 6 \\ &= 18.5 + 6 \\ &= 24.5 \\ BC &= 3x - 31 \\ &= 3(18.5) - 31 \\ &= 55.5 - 31 \\ &= 24.5 \end{aligned}$$



$$\begin{aligned} \overline{AB} &\cong \overline{BC} \\ 3(3x - 1) &= 5(2x + 2) \\ 9x - 3 &= 10x + 10 \\ -9x & \quad -9x \\ -3 &= x + 10 \\ -10 & \quad -10 \\ -13 &= x \end{aligned}$$

$$\begin{aligned} AB &= 3(3x - 1) \\ &= 3(-13 - 1) \\ &= 3(-14) \\ &= -42 \\ BC &= 5(2x + 2) \\ &= 5(-26 + 2) \\ &= 5(-24) \\ &= -120 \end{aligned}$$

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