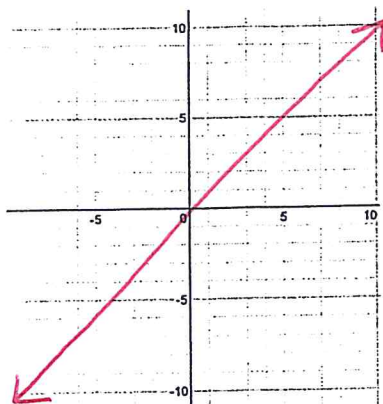


Family Functions Part 2 - Study Guide

Write the equation of the ~~transformed~~ parent functions (with a, h, k = values) and sketch its graph.

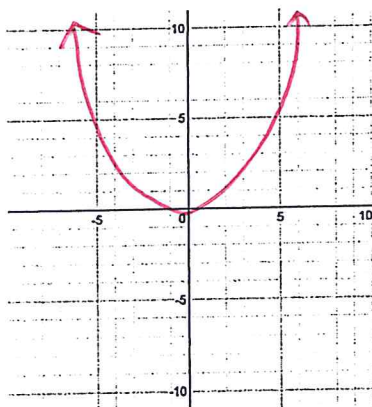
Linear

Equation: $f(x) = x$



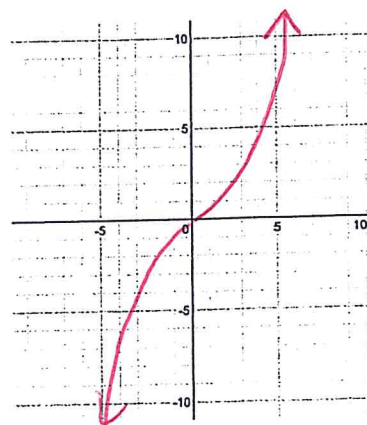
Polynomial Even

Equation: $f(x) = x^2$



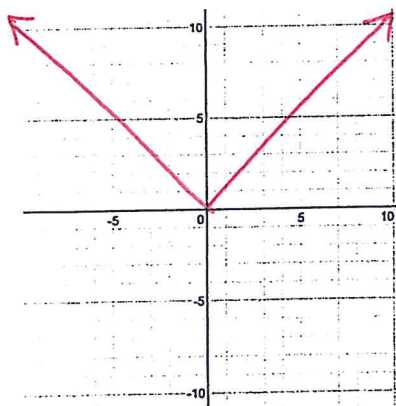
Polynomial Odd

Equation: $f(x) = x^3$



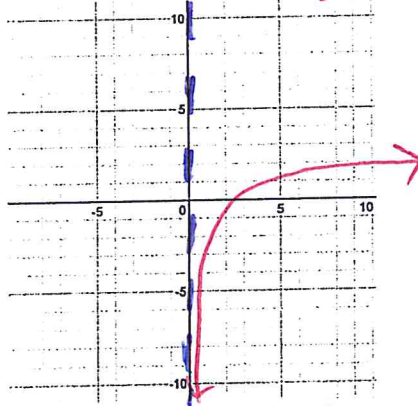
Absolute Value

Equation: $f(x) = |x|$

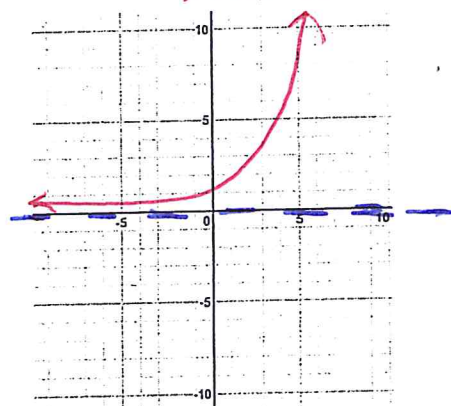


Logarithmic

Equation: $f(x) = \log x$

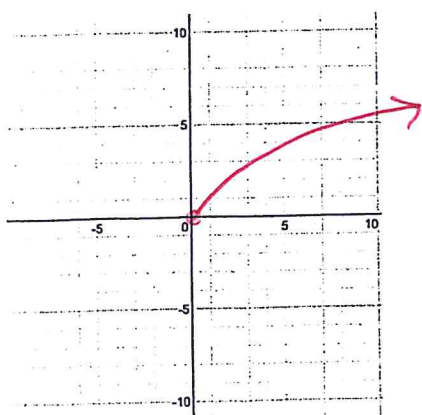


* Exponential ~~Decay~~ Growth
Equation: $f(x) = 2^x$

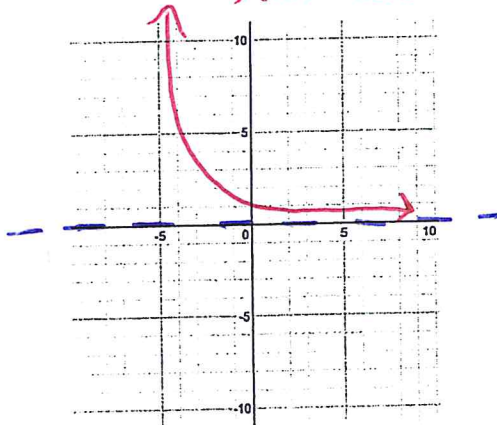


Radical Even

Equation: $f(x) = \sqrt{x}$

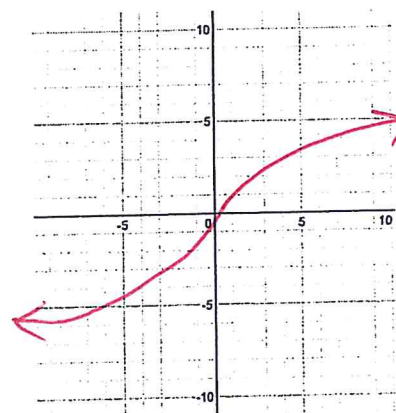


* Exponential ~~Growth~~ Decay
Equation: $f(x) = (\frac{1}{3})^x$



Radical Odd

Equation: $f(x) = \sqrt[3]{x}$



For #1 – 8 give the parent function name and equation, all a, h, and k values with their transformations.

1. $f(x) = 3 \log(x + 1) + 6$

~~Parent~~ Family Logarithm Parent Function Equation: $f(x) = \log x$

a – value: 3 Transformation(s): vertical stretch of 3

h – value: -1 Transformation: Translation 1L

k – value: 6 Transformation: Translation 6U

2. $g(x) = 0.4\sqrt[3]{x - 2}$

~~Parent~~ Family Radical Odd Parent Function Equation: $f(x) = \sqrt[3]{x}$

a – value: .4 Transformation(s): Vertical shrink of .4 or $\frac{2}{5}$

h – value: 2 Transformation: Translation 2R

k – value: 0 Transformation: —

3. $f(x) = -2x + 5$

~~Parent~~ Family Linear Parent Function Equation: $f(x) = x$

a – value: -2 Transformation(s): Vertical Reflection, Vertical Stretch of 2

h – value: 0 Transformation: —

k – value: 5 Transformation: Translation 5U

4. $f(x) = -\frac{2}{3}(x + 7)^2 - 4$

~~Parent~~ Family Polynomial even Parent Function Equation: $f(x) = x^2$

a – value: $-\frac{2}{3}$ Transformation(s): Vertical reflection, vertical shrink of $\frac{2}{3}$

h – value: -7 Transformation: Translation 7L

k – value: -4 Transformation: Translation 4D

5. $g(x) = \frac{1}{2}^{(x-3)} - 1$

~~Parent~~ ^{Family} Function Name: Exponential Decay

Parent Function Equation: $f(x) = (\frac{1}{2})^x$

a - value: 1 Transformation(s): —

h - value: 3 Transformation: Translation 3 R

k - value: -1 Transformation: Translation 1 D

6. $g(x) = 2^{(x-5)} - 6$

~~Parent~~ ^{Family} Function Name: Exponential Growth

Parent Function Equation: $f(x) = 2^x$

a - value: 1 Transformation(s): —

h - value: 5 Transformation: Translation 5 R

k - value: -6 Transformation: Translation 6 D

7. $g(x) = 0.4(x - 2)^3$

~~Parent~~ ^{Family} Function Name: Polynomial odd Parent Function Equation: $f(x) = x^3$

a - value: .4 Transformation(s): Vertical Shrink of .4

h - value: 2 Transformation: Translation 2 R

k - value: 0 Transformation: —

8. $f(x) = -\frac{1}{5}|x + 3| - 2$

~~Parent~~ ^{Family} Function Name: Absolute Value Parent Function Equation: $f(x) = |x|$

a - value: -1/5 Transformation(s): Vertical Reflection, vertical shrink of 1/5

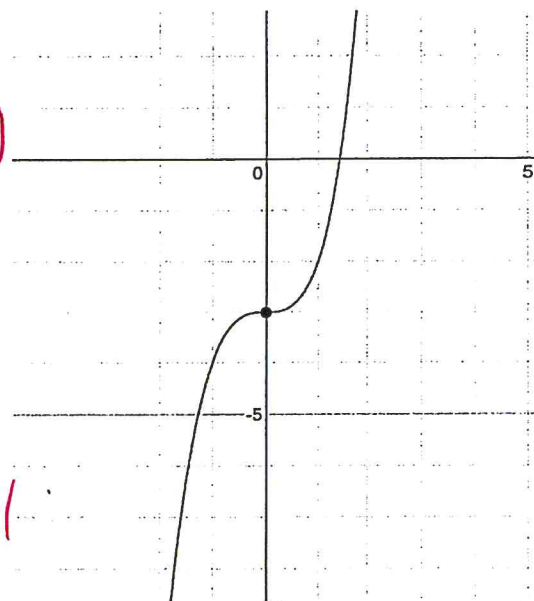
h - value: -3 Transformation: Translation 3 L

k - value: -2 Transformation: Translation 2 D

Find the transformed equation by using all the information from the graph and find the a-value. SHOW ALL WORK
 ***** If you are given only one point, that is the major point and the a value is 1. If you have two points then you must solve for a - value.

9. Family Name: Polynomial Odd $f(x) = x^3$
 a - value: 1 (2 points are not given!)
 h - value: 0
 k - value: -3 Translation 3D

Transformation Equation: $f(x) = x^3 - 3$



10. Family Name: Absolute Value $f(x) = |x|$
 a - value: ?
 h - value: 0
 k - value: 2

Translation 2U

Transformation Equation: $f(x) =$

$f(x) = -2|x - 0| + 2$

$f(x) = -2|x| + 2$

$$y = a|x - h| + k$$

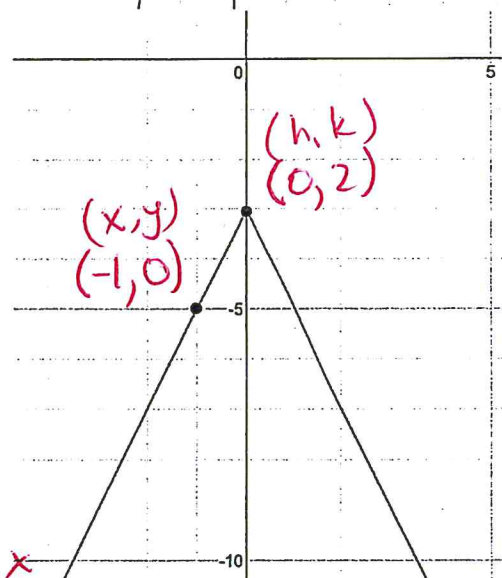
$$0 = a|-1 - 0| + 2$$

$$0 = a|-1| + 2$$

$$0 = |a| + 2$$

$$-2 = -2$$

$$a = -2$$

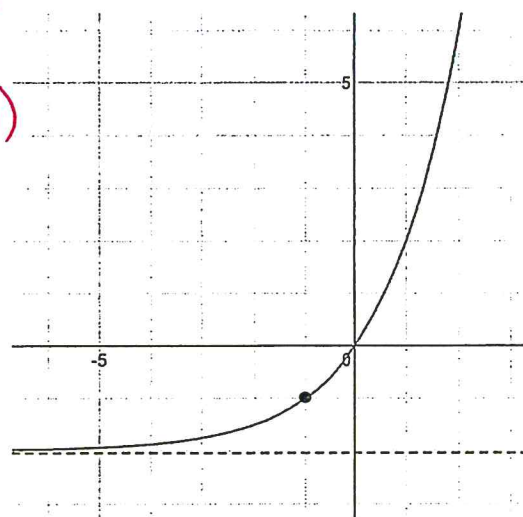


11. Family Name: Exponential Growth, $f(x) = 2^x$
 a - value: 1 (2 points are not given!)
 h - value: -1
 k - value: -2

$(0, 1) \rightarrow (-1, -1)$
 Translated
 1L, 2D

Transformation Equation: $f(x) = 2^{x-(-1)} - 2$

$f(x) = 2^{x+1} - 2$



12. Family Name: Radical Even - $f(x) = \sqrt{x}$
 a - value: ?
 h - value: -3 Translated 3L, 2U
 k - value: 2

Transformation Equation: $f(x) = a\sqrt{x-h} + k$

$$4 = a\sqrt{1 - (-3)} + 2$$

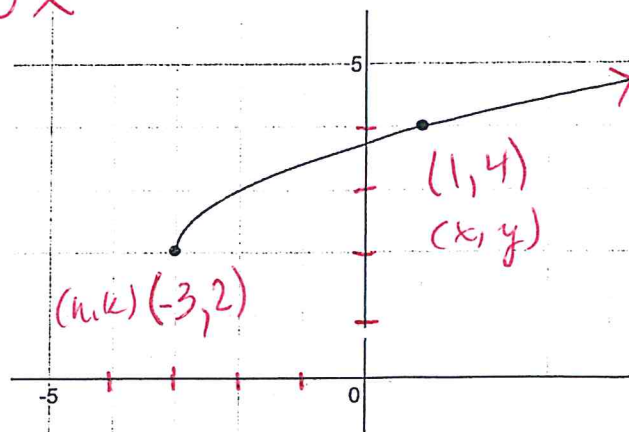
$$4 = a\sqrt{4} + 2$$

$$4 = 2a + 2$$

$$\frac{2a = 2}{2} \quad a = 1$$

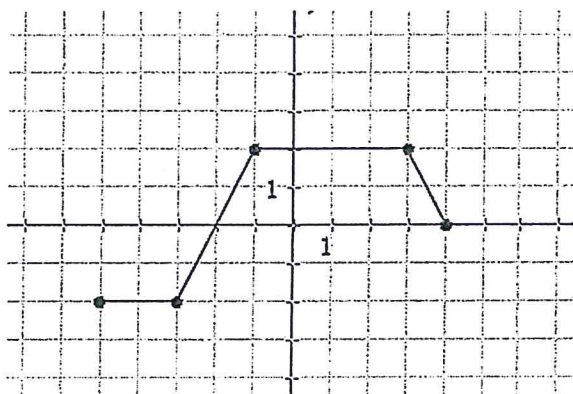
$$f(x) = \sqrt{x - (-3)} + 2$$

$$\boxed{f(x) = \sqrt{x+3} + 2}$$



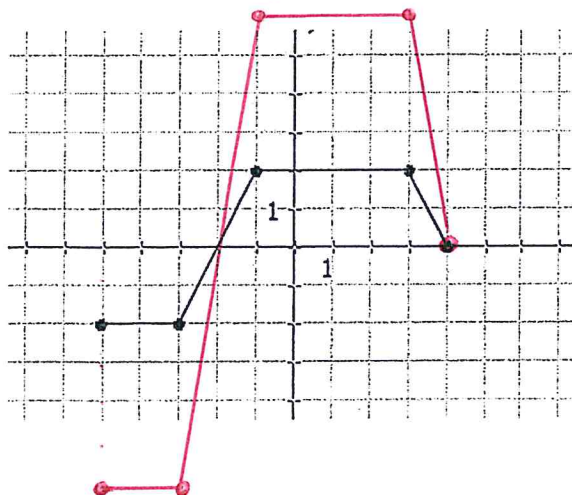
Use the following arbitrary graph of $y = f(x)$ to describe the transformations and sketch a graph of the transformed function.

13. Transform the arbitrary function in "a" for questions b and c.
 a. Create a table to represent this arbitrary function.



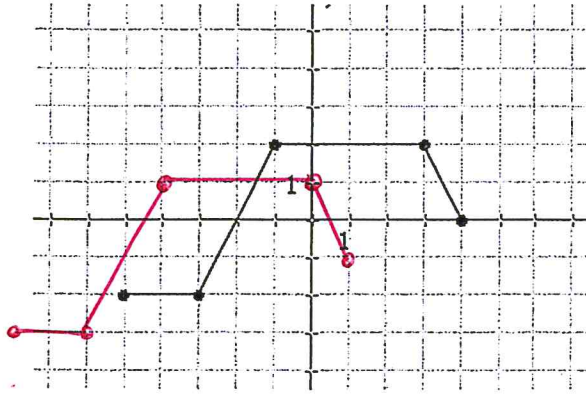
x	Y
-5	-2
-3	-2
-1	2
3	2
4	0

- b. $m(x) = 3f(x)$ $a=3, h=0, k=0$ Vertical Stretch of 3



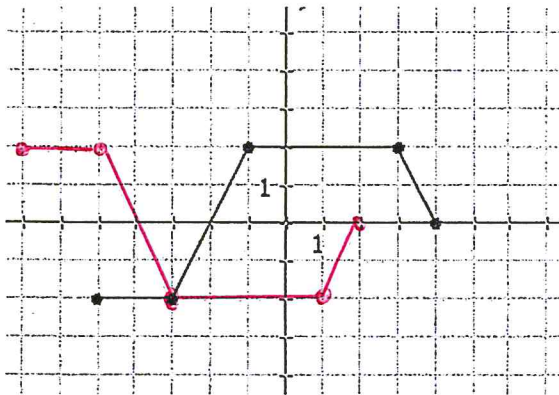
x	3Y
-5	-6
-3	-6
-1	6
3	6
4	0

c. $h(x) = f(x+3) - 1$ $a=1, h=-3, k=-1$ Translation 3L, 1D



$x-3$	$y-1$
-8	-3
-6	-3
-4	1
0	1
1	-1

d. $g(x) = -f(x+2)$ $a=-1, h=-2, k=0$ Vertical Reflection Translation 2D



x	$-y$	$x-2$	y
-5	2	-7	2
-3	2	-5	2
-1	-2	-3	-2
3	-2	1	-2
4	0	2	0