

# Polynomial odd + radical odd are inverses

## Radical

(Odd)

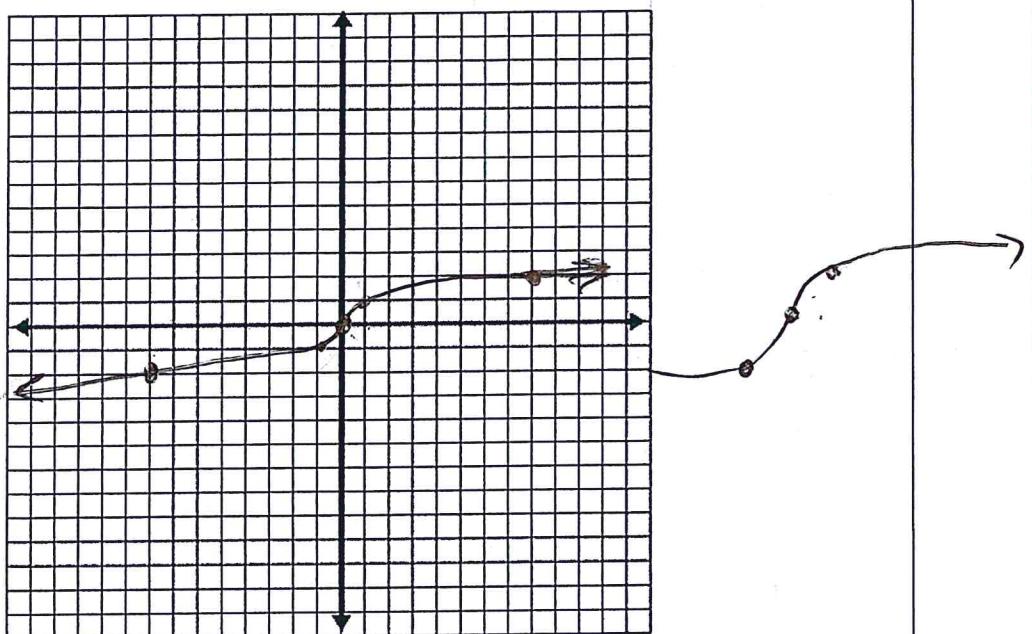
Example:  $f(x) = \sqrt[3]{x}$

Table of Values

choose two positive,  
two negative and zero  
for values of x

x	y
-8	-2
-1	-1
0	0
1	1
8	2

Sketch:



$f(x) =$

Domain  
(interval)

$$(-\infty, \infty)$$

Range  
(interval)

$$(-\infty, \infty)$$

Increasing  
(interval)

$$(-\infty, \infty)$$

Decreasing  
(interval)

— | constant —

X-  
Intercept(s)

$$(0, 0)$$

Y-  
Intercept(s)

$$(0, 0)$$

Asymptotes

—

End behavior

L: As  $x \rightarrow -\infty, y \rightarrow -\infty$

R: As  $x \rightarrow \infty, y \rightarrow \infty$

Additional info:

$$f(x) = b^x \quad b > 1$$

$$2^x \neq 0$$

### Exponential Growth

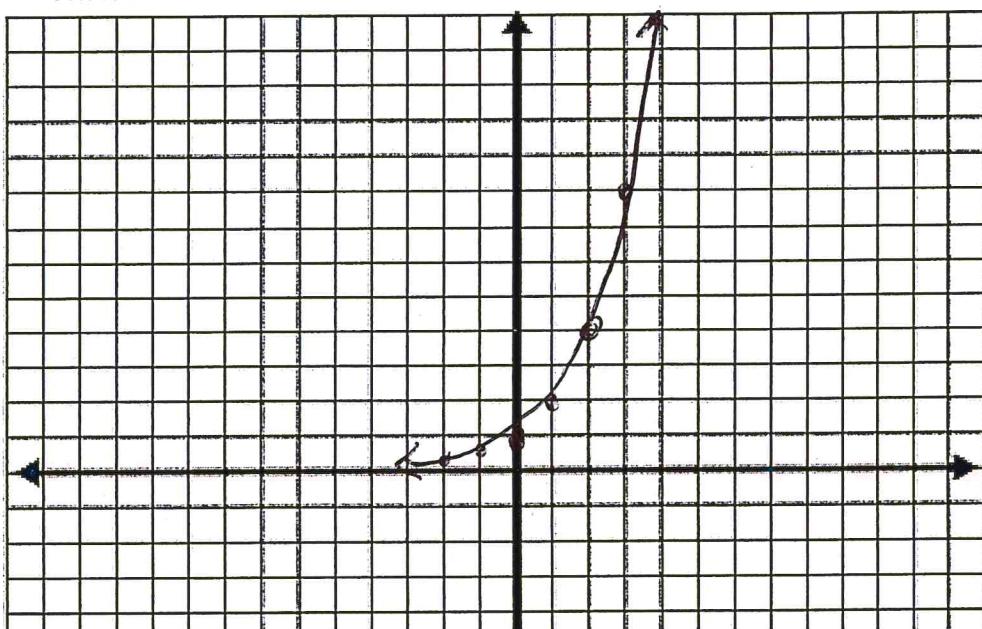
Example:  $f(x) = 2^x$

Table of Values

choose two positive,  
two negative and zero  
for values of  $x$

$x$	$y$
-2	$2^{-2} = \frac{1}{4}$
-1	$2^{-1} = \frac{1}{2}$
0	$2^0 = 1$
1	$2^1 = 2$
2	$2^2 = 4$

Sketch:



$f(x) = 2^x$

Domain  
(interval)

$$(-\infty, \infty)$$

Range  
(interval)

$$(0, \infty)$$

Increasing  
(interval)

$$(-\infty, \infty)$$

Decreasing  
(interval)

—      | constant —

X-  
Intercept(s)

—

Y-  
Intercept(s)

$$(0, 1)$$

Asymptotes

HA

$x\text{-axis}$

$$y = 0$$

End behavior

L: As  $x \rightarrow -\infty, y \rightarrow 0$

R: As  $x \rightarrow \infty, y \rightarrow \infty$

Additional info:

$0 < b < 1$  Decay

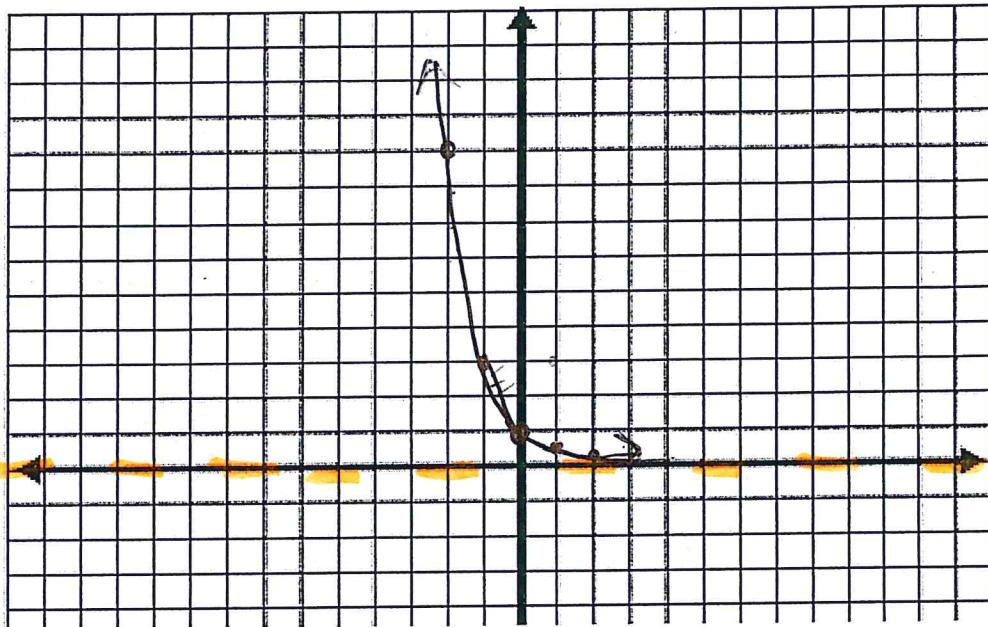
**Exponential Decay**  
 $f(x) = \left(\frac{1}{3}\right)^x$

Table of Values

choose two positive,  
two negative and zero  
for values of x

x	y
-2	$\left(\frac{1}{3}\right)^{-2} = 9$
-1	$\left(\frac{1}{3}\right)^{-1} = 3$
0	$\left(\frac{1}{3}\right)^0 = 1$
1	$\left(\frac{1}{3}\right)^1 = \frac{1}{3}$
2	$\left(\frac{1}{3}\right)^2 = \frac{1}{9}$

Sketch:



Domain (interval)	$(-\infty, \infty)$	
Range (interval)	$(0, \infty)$	
Increasing (interval)	—	
Decreasing (interval)	$(-\infty, \infty)$	constant —
X-Intercept(s)	—	
Y-Intercept(s)	$(0, 1)$	
Asymptotes	HA at $\boxed{y=0}$ (x-axis)	
End behavior	L: As $x \rightarrow -\infty$ , $y \rightarrow \infty$ R: As $x \rightarrow \infty$ , $y \rightarrow 0$	

Additional info:

Add'l info: Logs are inverses of exponentials  $\log_{10}x$   
common log

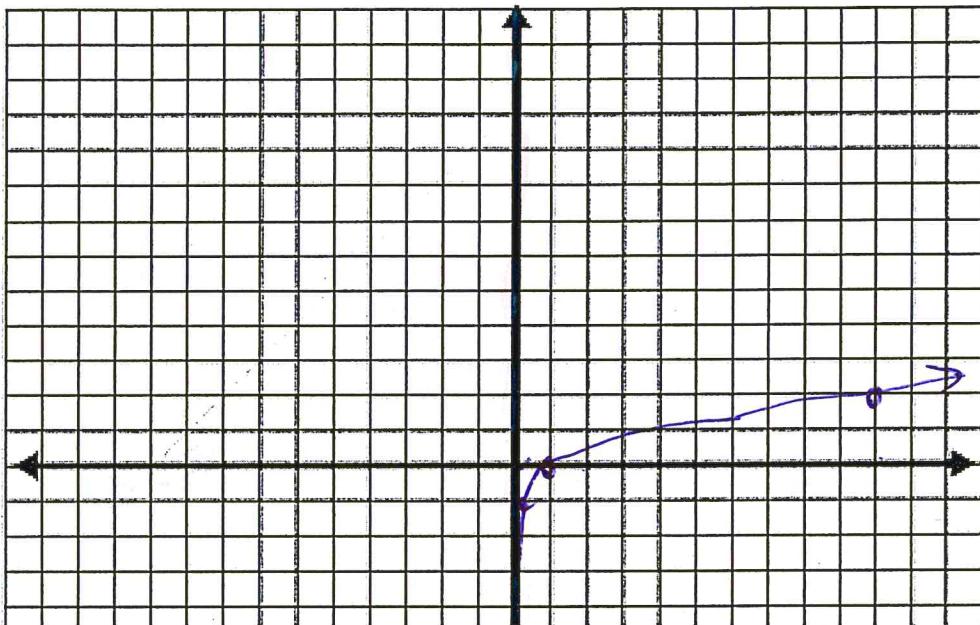
### Logarithm $f(x) = \log x$

Table of Values

choose two positive,  
two negative and zero  
for values of x

x	y
100	-2
10	-1
1	0
10	1
100	2

Sketch:



Domain (interval)	$(0, \infty)$	
Range (interval)	$(-\infty, \infty)$	
Increasing (interval)	$(0, \infty)$	
Decreasing (interval)	—   constant —	
X-Intercept(s)	$(1, 0)$	
Y-Intercept(s)	—	
Asymptotes	VA at $x=0$ (y-axis)	
End behavior L:	As $x \rightarrow 0, y \rightarrow -\infty$	
R:	As $x \rightarrow \infty, y \rightarrow \infty$	

Additional info: