

1. $(a - b)^2 = a^2 - 2ab + b^2$

a) working left side:

$$(a - b)^2$$

$$(a - b)(a - b)$$

$$a^2 - ab - ab + b^2$$

$$a^2 - 2ab + b^2 = \underbrace{a^2 - 2ab + b^2}_{\text{right side}}$$

working right side:

$$a^2 - 2ab + b^2$$

$$\underline{a^2 - ab} - \underline{ab + b^2}$$

$$\underline{a(a - b) - b(a - b)}$$

$$(a - b)(a - b)$$

$$(a - b)^2 = \underbrace{(a - b)^2}_{\text{left side}}$$

2. $a^3 + b^3 = (a + b)(a^2 - ab + b^2)$

a) working right side:

$$(a + b)(a^2 - ab + b^2)$$

$$a^3 - \underline{a^2b} + \underline{ab^2} + \underline{a^2b} - \underline{ab^2} + b^3$$

$$a^3 + b^3 = \underbrace{a^3 + b^3}_{\text{left side}}$$

3. $(ax + b)(x + a) = ax^2 + a^2x + bx + ab$

a) working left side:

$$(ax + b)(x + a)$$

$$ax^2 + a^2x + bx + ab = \underbrace{ax^2 + a^2x + bx + ab}_{\text{side}}$$

working right side

$$\underline{ax^2 + a^2x} + \underline{bx + ab}$$

$$\underline{ax(x + a) + b(x + a)}$$

$$(x + a)(ax + b)$$

$$(ax + b)(x + a) = \underbrace{(ax + b)(x + a)}_{\text{left side}}$$

4. $(a + b)^3 = a^3 + b^3 + 3a^2b + 3ab^2$

a) working left side

$$(a + b)^3$$

$$(a + b)(a + b)(a + b)$$

$$(a^2 + ab + ab + b^2)(a + b)$$

$$(a^2 + 2ab + b^2)(a + b)$$

$$a^3 + \underline{2a^2b} + \underline{ab^2} + \underline{a^2b} + \underline{2ab^2} + b^3$$

$$a^3 + b^3 + 3a^2b + 3ab^2 = \underbrace{a^3 + b^3 + 3a^2b + 3ab^2}_{\text{right side}}$$

working right side:

$$\underline{a^3 + b^3} + \underline{3a^2b + 3ab^2}$$

$$\underline{(a + b)(a^2 - ab + b^2) + 3ab(a + b)}$$

$$(a + b)(a^2 - ab + b^2 + 3ab)$$

$$(a + b)(a^2 + 2ab + b^2) \leftarrow \text{PST}$$

$$(a + b)(a + b)(a + b)$$

$$(a + b)^3 = \underbrace{(a + b)^3}_{\text{left side}}$$