

1. Draw triangle in correct quad
2. Label sides using given info
3. Use Pythagorean Thm to get 3rd side
4. Find other trig ratios
5. Verify identity using ratios

Example 2

Given $\sin \theta = -\frac{2}{5}$ in QIII, find $\cos \theta$ & $\tan \theta$, then verify

$$\begin{aligned} x^2 + (-2)^2 &= 5^2 \\ x^2 + 4 &= 25 \\ x^2 &= 21 \\ x &= \sqrt{21} \end{aligned}$$

$$\begin{aligned} \left(-\frac{2}{5}\right)^2 + \left(\frac{\sqrt{21}}{5}\right)^2 &= 1 \\ \frac{4}{25} + \frac{21}{25} &= \frac{25}{25} = 1 \quad \checkmark \end{aligned}$$

$$\cos \theta = -\frac{\sqrt{21}}{5} \quad \tan \theta = \frac{-2}{\sqrt{21}} \cdot \frac{\sqrt{21}}{\sqrt{21}} = \frac{2\sqrt{21}}{21}$$

Example 3

Given $\tan \theta = -5$ in QII, find others & verify.

$$\begin{aligned} 5^2 + (-1)^2 &= c^2 \\ c^2 &= 25 + 1 \\ c^2 &= 26 \\ c &= \sqrt{26} \end{aligned}$$

$$\begin{aligned} \left(\frac{5}{\sqrt{26}}\right)^2 + \left(\frac{-1}{\sqrt{26}}\right)^2 &= 1 \\ \frac{25}{26} + \frac{1}{26} &= \frac{26}{26} = 1 \quad \checkmark \end{aligned}$$

$$\sin \theta = \frac{5}{\sqrt{26}} \cdot \frac{\sqrt{26}}{\sqrt{26}} = \frac{5\sqrt{26}}{26}$$

$$\cos \theta = -\frac{1}{\sqrt{26}} \cdot \frac{\sqrt{26}}{\sqrt{26}} = -\frac{\sqrt{26}}{26}$$