

Synthetic Division

When Does it work? In order to divide polynomials using synthetic division, you must be dividing by a **linear expression** and the **leading coefficient** (first number) **must be a 1**. For example, you can use synthetic division to divide by $x + 3$ or $x - 6$, but you cannot use synthetic division to divide by $x^2 + 2$ or $6x + 7$.

$$\begin{array}{r} \text{Divisor} \\ -3x - 2 \quad L \\ x^2 + 2 \quad L \\ x - 3 \quad S \end{array}$$

How Does it work?

- Step 1:** To set up the problem, first, Make a long "L" and put **all** of the **coefficients** of your dividend at the top. make sure the numerator is written in descending order and if any terms are missing you must use a zero to fill in the missing term.

$$\begin{array}{r} x^3 - 4x^2 - 3x + 6 \quad \leftarrow \text{dividend} \\ x - 2 \quad \leftarrow \text{divisor} \\ \hline = x^2 - 2x - 7 - \frac{8}{x-2} \end{array}$$

$$\begin{array}{r|rrrr} & x^3 & x^2 & x & & \\ & 1 & -4 & -3 & 6 & \\ \downarrow & & 2 & -4 & -14 & \\ \hline & 1x^2 & -2x & -7 & -8 & R \end{array}$$

- Step 2:** Change the sign of your divisor, drop the x.
- Step 3:** Once the problem is set up correctly, bring the leading coefficient (first number) straight down.
- Step 4:** Multiply the number in the division box with the number you brought down and put the result in the next column.
- Step 5:** Add the two numbers together and write the result in the bottom of the row. Repeat until done.
- Step 6:** To write the final answer, reduce the exponent by 1 and then use the numbers under the "L" as your coefficients. The last number is the remainder and the remainder must be written as a fraction.

$$\begin{array}{r} 0x^3 \\ = x^3 - 2x^2 - 3 + \frac{12}{x+2} \quad \leftarrow \text{dividend} \\ x + 2 \quad \leftarrow \text{divisor} \\ \hline = x^2 + x - 1 + \frac{18}{x+3} \quad \leftarrow \text{dividend} \\ x + 3 \quad \leftarrow \text{divisor} \\ \hline \end{array}$$

$$\begin{array}{r|rrrr} -2 & x^4 & x^3 & x^2 & x & \\ & 1 & 0 & -4 & -3 & 6 \\ \downarrow & & -2 & +4 & 0 & 6 \\ \hline & 1x^3 & -2x^2 & 0x & -3 & 12 R \end{array}$$

$$\begin{array}{r|rrrr} -3 & x^3 & x^2 & x & & \\ & 1 & 4 & -1 & 6 & \\ \downarrow & & -3 & -3 & 12 & \\ \hline & 1x^2 & 1x & -4 & 18 & R \end{array}$$