

SAT Wednesday 02/28

Number of Contestants by Score and Day

	5 out of 5	4 out of 5	3 out of 5	2 out of 5	1 out of 5	0 out of 5	Total
Day 1	2	3	4	6	2	3	20
Day 2	8	3	5	5	4	1	20
Day 3	3	3	4	5	3	2	20
Total	7	9	13	16	9	6	60

The same 20 contestants, on each of 3 days, answered 5 questions in order to win a prize. Each contestant received 1 point for each correct answer. The number of contestants receiving a given score on each day is shown in the table above.

$$2 \cdot 5 = 10$$

$$3 \cdot 4 = 12$$

$$4 \cdot 3 = 12$$

$$6 \cdot 2 = 12$$

$$2 \cdot 1 = 2$$

$$3 \cdot 0 = 0$$

$$\frac{48}{48}$$

$$\frac{48}{20} = 2.4$$

$$\frac{2+3}{7}$$

$$\frac{5}{7}$$

37

What was the mean score of the contestants on Day 1?

No contestant received the same score on two different days. If a contestant is selected at random, what is the probability that the selected contestant received a score of 5 on Day 2 or Day 3, given that the contestant received a score of 5 on one of the three days?

$$2) \frac{1 + \tan(\frac{\pi}{2} - x) \csc x}{\csc^2 x} = \frac{\cot x \cdot \csc x}{\csc^2 x} = \frac{\cos x}{\sin^2 x}$$

$$\frac{\cos x}{\sin^2 x} \cdot \frac{\sin^2 x}{1} = \frac{\cos x}{1} = \boxed{\cos x}$$

$$(24) \frac{1 + \tan x}{1 + \cot x} = \frac{1 + \tan x}{\frac{1}{1} + \frac{1}{\tan x}} = \frac{1 + \tan x}{\frac{\tan x + 1}{\tan x}} = (1 + \tan x) \cdot \frac{\tan x}{\tan x + 1} = \tan x$$

(I12)

$$1 + \tan^2 x = \sec^2 x$$

$$1 + \tan x = \sec \text{ NO.}$$

$$25) (\sec^2 x + \csc^2 x) - (\tan^2 x + \cot^2 x)$$

$$1 + \tan^2 x + 1 + \cot^2 x - \tan^2 x - \cot^2 x$$

$$1 + 1 = 2$$

$$\begin{aligned}
 26) \quad \frac{\sec^2 u - \tan^2 u}{\cos^2 u + \sin^2 u} &= \sec^2 u - \tan^2 u \\
 &= 1 \tan^2 u - \tan^2 u \\
 &= 1 \cdot \checkmark
 \end{aligned}$$

(12)

(10)

$$\begin{aligned}
 27) \quad &(\sin x)(\tan x + \cot x) \\
 &\sin x \left(\frac{\tan x}{1} + \frac{1}{\tan x} \right) = \frac{\tan^2 x}{\tan} + \frac{1}{\tan x} = \frac{\tan^2 x + 1}{\tan x} = \frac{\sec^2 x}{\tan x} \\
 &\sin x \left(\frac{\sec^2 x}{\tan x} \right) = \sin x \cdot \frac{\frac{1}{\cos^2 x}}{\frac{\sin x}{\cos x}} = \frac{1}{\cos x} \cdot \frac{\cos x}{\sin x} = \frac{1}{\cos x} \cdot \frac{1}{\sin x} \\
 &\sin x \left(\frac{1}{\cos x \cdot \sin x} \right) = \\
 &\frac{\sin x}{1} \times \frac{1}{\cos x \cdot \sin x} = \frac{\sin x}{\cos x \cdot \sin x} = \frac{1}{\cos x} = \sec x
 \end{aligned}$$

$$\begin{aligned}
 27) \quad &\sin x (\tan x + \cot x) \\
 &\sin x \left(\frac{\sin x}{\cos x} + \frac{\cos x}{\sin x} \right) \\
 &\frac{\sin^2 x}{\cos x} + \frac{\sin x \cos x \cdot \cos x}{\sin x \cdot \cos x} = \frac{\sin^2 x + \cos^2 x}{\cos x} = \frac{1}{\cos x} = \sec x
 \end{aligned}$$

$$\begin{aligned}
 28) \quad &\sin \theta - \tan \theta \cos \theta + \cos(\pi/2 - \theta) \\
 &\sin \theta - \frac{\sin}{\cos} (\cos) + \sin \theta \\
 &\sin \theta - \sin \theta + \sin \theta
 \end{aligned}$$

(Sino)

29) $\sin x \cos x \tan x \sec x \csc x$

$$\sin x \cdot \cos x \cdot \tan x \cdot \frac{1}{\cos x} \cdot \frac{1}{\sin x} = \tan x$$

30) $\frac{(\sec y - \tan y)(\sec y + \tan y)}{\sec y}$

I 12
 $1 + \tan^2 = \sec^2$
 $\sec^2 - \tan^2 = 1$

$$\frac{(\sec^2 y) - (\tan^2 y)}{\frac{1}{\cos y}}$$

$$\frac{1}{\frac{1}{\cos y}}$$

$$\frac{1}{1} \cdot \cos y$$

$y = \cos y$