

Converting to vertex form

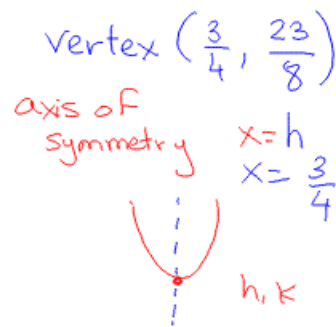
- $y = 2x^2 - 3x + 4$ $a=2$ $b=-3$ $c=4$
- $h = \frac{-b}{2a}$
- To find K plug in h for x in the standard form, k is the y

vertex (h, k)

$$\left(\frac{3}{4}, ?\right)$$

$$h = -\frac{b}{2a} = \frac{3}{2 \cdot 2} = \frac{3}{4}$$

$$\begin{aligned} & 2x^2 - 3x + 4 \\ & 2\left(\frac{3}{4}\right)^2 - 3\left(\frac{3}{4}\right) + 4 \\ & = 2 \cdot \frac{9}{16} - \frac{9 \cdot 2}{4} + \frac{4 \cdot 8}{1 \cdot 8} \\ & = \frac{9 - 18 + 32}{8} = \frac{23}{8} \leftarrow k. \end{aligned}$$



Vertex form:

$$f(x) = a(x-h)^2 + k.$$

↓
same as "a" in standard form

$$= 2\left(x - \frac{3}{4}\right)^2 + \frac{23}{8}$$

Write the following function in vertex form

• $f(x) = 6x - 3x^2 - 5$

$$f(x) = -3x^2 + 6x - 5$$

$$a = -3 \quad b = 6 \quad c = -5 \quad (h, k)$$

$$h = \frac{-b}{2a}$$

$$h = \frac{-6}{2(-3)}$$

$$h = \frac{-6}{-6} = 1$$

$$-3(1)^2 + 6(1) - 5 \quad (1, ?)$$

$$-3 + 6 - 5 = -2 \quad (1, -2)$$

vertex form $a \cdot (x-h)^2 + k$

$$f(x) \quad g(x) = -3(x-1)^2 - 2$$

$x=1$ axis of symmetry.

To describe the graph of a Quadratic Function

- Vertex (h, k)
- Axis of the parabola (axis of symmetry) $x=h$
- Parabola opens upward ($a>0$) parabola opens downward ($a<0$)
- Initial value (y intercept) : $f(0)=c$
- X intercepts (quadratic formula)

• $f(x) = 6x - 3x^2 - 5$

$$f(x) = -3(x-1)^2 - 2$$

- vertex $(1, -2)$
- axis of symmetry $x=h$ $x=1$
- $\cup \cap$? downward $a < 0$
- y-int -5 (c from the standard form)
- x-int

$$f(x) = -3x^2 + 6x - 5$$

$$x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a} = \frac{-6 \pm \sqrt{36 - 4(-3)(-5)}}{-6}$$

$$= \frac{-6 \pm \sqrt{-24}}{-6} = \frac{-6 \pm \sqrt{4 \cdot 6i}}{-6}$$

$$= \frac{-6 \pm 2\sqrt{6i}}{-6 \div 2} = \frac{-6 \pm 2\sqrt{6i}}{-3}$$

$$= \frac{-3 \pm \sqrt{6i}}{-3}$$

No real
Solutions
the parabola
does not cross
the x-axis.

