Notes 5 – Statistics Name \_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_

Measuring Variability for Skewed Distributions (IQR)

Exploratory Challenge 1/Exercises 1–3: Skewed Data and its Measure of Center

Consider the following scenario. A television game show, *Fact or Fiction*, was canceled after nine shows. Many people watched the nine shows and were rather upset when it was taken off the air. A random sample of 30 viewers of the show was selected. Viewers in the sample responded to several questions. The dot plot below shows the distribution of ages of these 30 viewers.



1. Approximately where would you locate the mean (balance point) in the above distribution?
2. How does the direction of the tail affect the location of the mean age compared to the median age?
3. The mean age of the above sample is approximately. Do you think this age describes the typical viewer of this show? Explain your answer.

Exploratory Challenge 2/Exercises 4–8: Constructing and Interpreting the Box Plot

1. Using the above dot plot, construct a box plot over the dot plot by completing the following steps:
	* 1. Locate the middle observations, and draw a box around these values.
		2. Calculate the median, and then draw a line in the box at the location of the median.
		3. Draw a line that extends from the upper end of the box to the largest observation in the data set.
		4. Draw a line that extends from the lower edge of the box to the minimum value in the data set.
2. The values used to construct the box plot make up the -number summary. What is the -number summary for this data set of ages?

|  |  |
| --- | --- |
| Minimum age: |  |
| Lower quartile or Q1: |  |
| Median Age: |  |
| Upper quartile or Q3: |  |
| Maximum age: |  |

1. What percent of the data does the box part of the box plot capture?
2. What percent of the data falls between the minimum value and Q1?
3. What percent of the data falls between Q3 and the maximum value?

Exercises 9–14

An advertising agency researched the ages of viewers most interested in various types of television ads. Consider the following summaries:

|  |  |
| --- | --- |
| **Ages** | **Target Products or Services** |
| – | Electronics, home goods, cars |
| – | Financial services, appliances, furniture |
| – | Retirement planning, cruises, health care services |

1. The mean age of the people surveyed is approximately years old. As a result, the producers of the show decided to obtain advertisers for a typical viewer of years old. According to the table, what products or services do you think the producers will target? Based on the sample, what percent of the people surveyed about the *Fact or Fiction* show would have been interested in these commercials if the advertising table is accurate?
2. The show failed to generate the interest the advertisers hoped. As a result, they stopped advertising on the show, and the show was cancelled. Kristin made the argument that a better age to describe the typical viewer is the median age. What is the median age of the sample? What products or services does the advertising table suggest for viewers if the median age is considered as a description of the typical viewer?
3. What percent of the people surveyed would be interested in the products or services suggested by the advertising table if the median age were used to describe a typical viewer?
4. What percent of the viewers have ages between Q1 and Q3? The difference between Q3 and Q1, or Q3 – Q1, is called the **interquartile range**, or **IQR**. What is the interquartile range (IQR) for this data distribution?
5. The IQR provides a summary of the variability for a skewed data distribution. The IQR is a number that specifies the length of the interval that contains the middle half of the ages of viewers. Do you think producers of the show would prefer a show that has a small or large interquartile range? Explain your answer.
6. Do you agree with Kristin’s argument that the median age provides a better description of a typical viewer? Explain your answer.

Exploratory Challenge 3/Exercises 15–20: Outliers

 Students at Waldo High School are involved in a special project that involves communicating with people in Kenya. Consider a box plot of the ages of randomly selected people from Kenya.



**A data distribution may contain extreme data (specific data values that are unusually large or unusually small relative to the median and the interquartile range). A box plot can be used to display extreme data values that are identified as outliers.**

**Each “\*” in the box plot represents the ages of four people from this sample. Based on the sample, these four ages were considered outliers.**

1. Estimate the values of the four ages represented by an \*.

**An outlier is defined to be any data value that is more than away from the nearest quartile.**

1. What is the median age of the sample of ages from Kenya? What are the approximate values of Q1 and Q3? What

 is the approximate IQR of this sample?

1. Multiply the IQR by . What value do you get?
2. Add to the 3rd quartile age (Q3). What do you notice about the four ages identified by an \*?
3. Are there any age values that are less than ? If so, these ages would also be considered outliers.